

Dynamical Phenomena in 2D Yukawa Systems

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Overview



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- Method: utilize N -body code (`box_tree`) to simulate realistic complex plasma crystals

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- Method: utilize N -body code (`box_tree`) to simulate realistic complex plasma crystals
- Specific aims:
 - Anomalous diffusion
 - Self-organization

Diffusion Phenomena

Simulating an Experimental Crystal

- Meyer, et al. give the following experimental parameters for a complex plasma crystal:

Grain Diameter	$d \approx 9 \mu\text{m}$
Grain Charge	$Q \approx -2 \times 10^4 e$
Kappa	$\kappa \approx 1.3$
Spacing	$a \approx 0.6 \text{ mm}$
Pressure	0.10-1.00 Pa
RF Power	25-200 W
Self-Bias	(-10)-(-40) V
T_e	1.5-7 eV
N_e	10^{14} - 10^{15} m^{-3}

Meyer, J., Laut, I., Zhdanov, S., Nosenko, V. and Thomas, H. (2017). Coupling of Noncrossing Wave Modes in a Two-Dimensional Plasma Crystal. *Physical Review Letters*, 119(25).

Simulating an Experimental Crystal



- Under these conditions, Meyer, et al. obtained a crystal of approximate diameter 27 cm

Simulating an Experimental Crystal



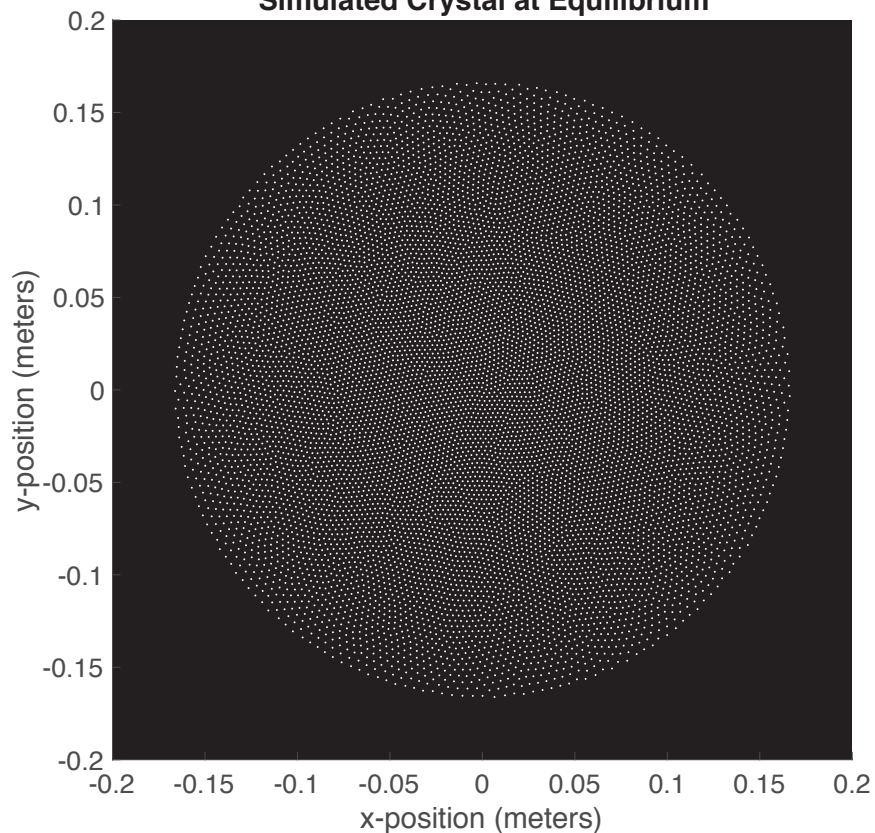
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- Under these conditions, we obtained a crystal of approximate diameter 32 cm

Simulating an Experimental Crystal

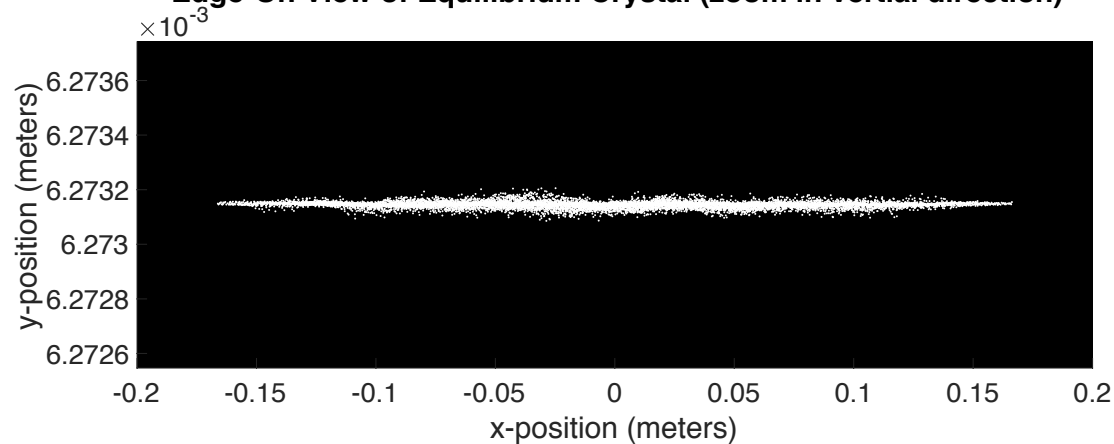
CASPER

www.baylor.edu/CASPER

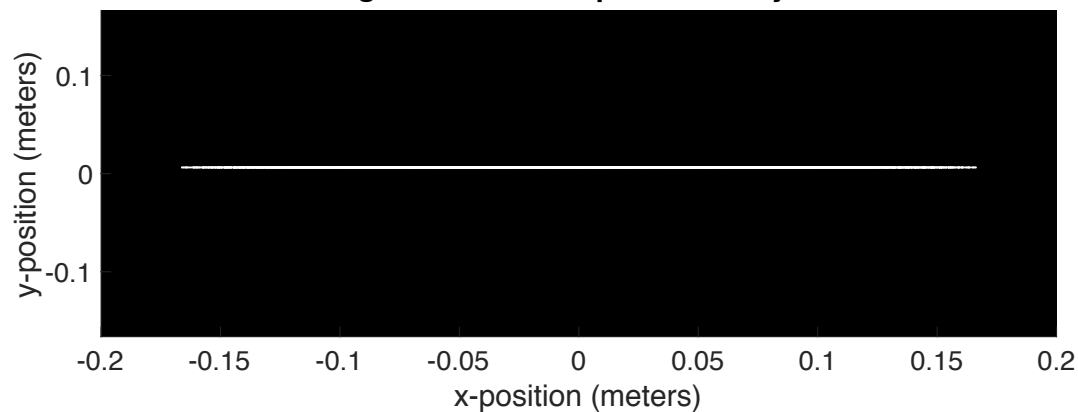
Simulated Crystal at Equilibrium



Edge-On View of Equilibrium Crystal (zoom in vertical direction)



Edge-On View of Equilibrium Crystal



Characterizing Diffusion

- Mean-Squared Displacement (MSD)

$$\text{MSD}(t) = \left\langle |\mathbf{r}_i(t) - \mathbf{r}_i(0)|^2 \right\rangle_{i=1}^N$$

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$$\text{MSD} \propto t^\alpha \begin{cases} \alpha > 1 \implies \text{superdiffusion} \\ \alpha = 1 \implies \text{normal diffusion} \\ \alpha < 1 \implies \text{subdiffusion} \end{cases}$$

Diffusion in 2D Yukawa Systems



- Liu, Goree, and Vaulina¹ use a molecular dynamics simulation to show that

$$88 < \Gamma < 145 \implies \text{normal diffusion}$$

¹Liu, B., Goree, J. and Vaulina, O. (2006). Test of the Stokes-Einstein Relation in a Two-Dimensional Yukawa Liquid. *Physical Review Letters*, 96(1).

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$$\Gamma = \frac{Q_{\text{grain}}^2}{4\pi\epsilon_0 r_{\text{Wigner-Seitz}} k_B T_{\text{grain}}}$$

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Diffusion in 2D Yukawa Systems



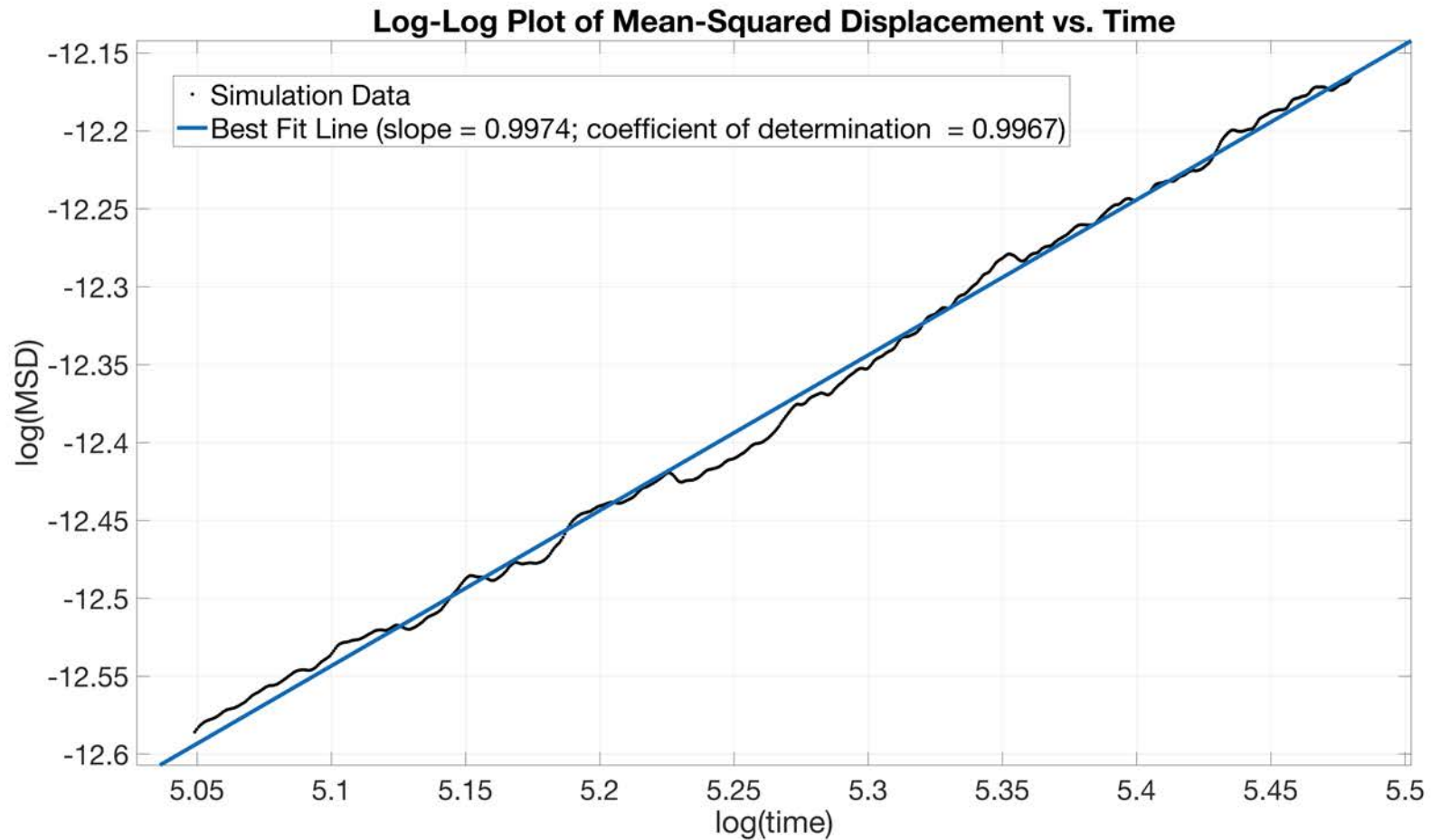
- To observe normal diffusion, we adjust Γ by adjusting the grain temperature

Diffusion in 2D Yukawa Systems

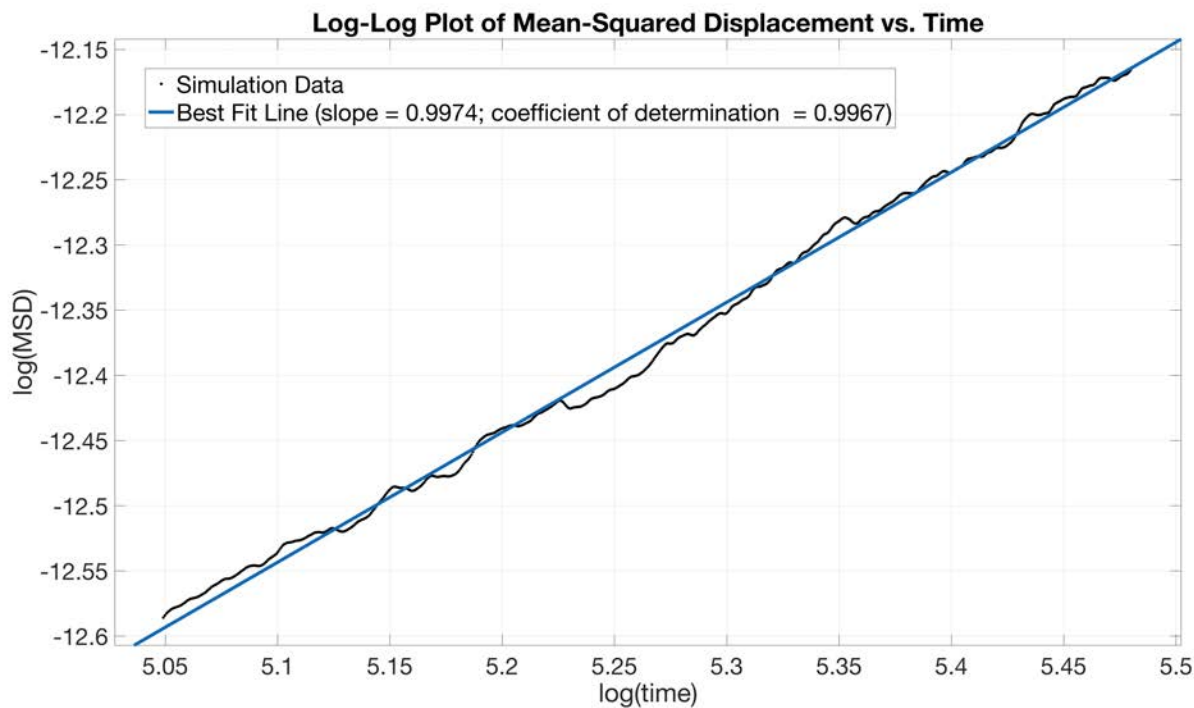
- To observe normal diffusion, we adjust Γ by adjusting the grain temperature
- The slope of the log-log plot of MSD vs. time indicates the diffusion regime

$$\text{MSD} \propto t^\alpha \left\{ \begin{array}{l} \alpha > 1 \implies \text{superdiffusion} \\ \alpha = 1 \implies \text{normal diffusion} \\ \alpha < 1 \implies \text{subdiffusion} \end{array} \right.$$

Observed Normal Diffusion

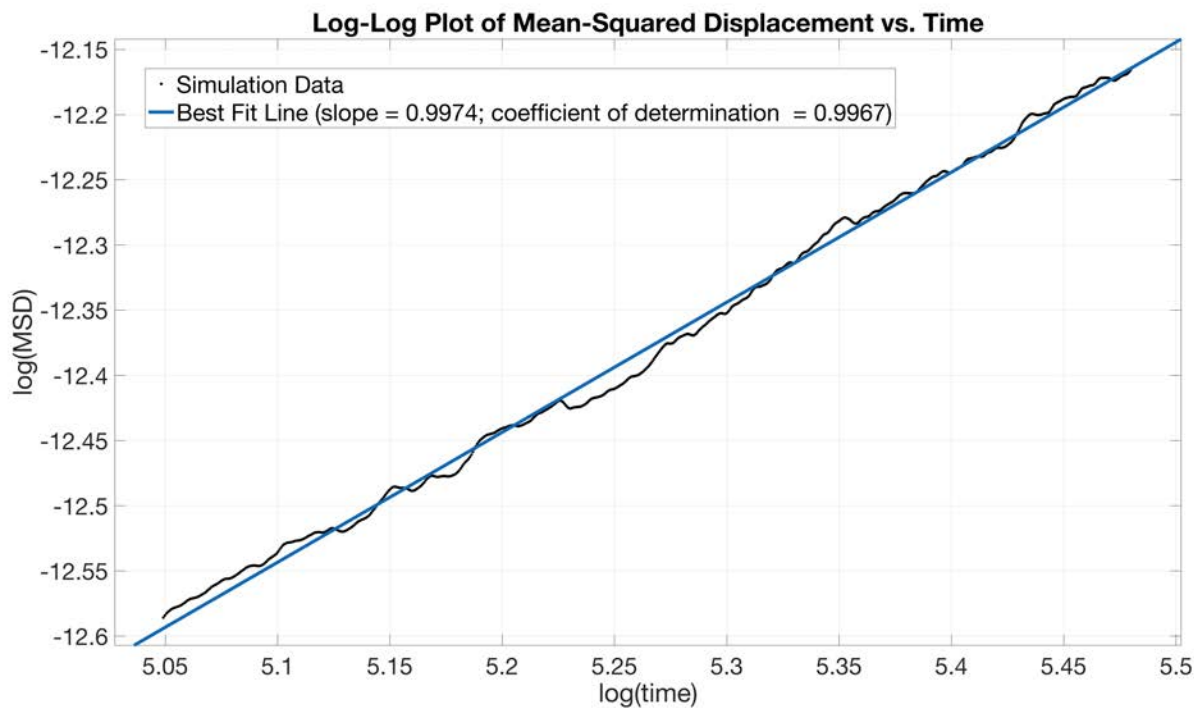


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$$\alpha = 0.9974 \approx 1$$

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\implies normal diffusion

$$\Gamma \approx 170$$

Diffusion in 2D Yukawa Systems



- We observe diffusive motion at a higher coupling parameter than Liu and Goree

Diffusion in 2D Yukawa Systems



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- (They only simulated Yukawa systems with $\Gamma < 145$)

Self-Organization

Choice of System Parameters



- We simulate a crystal using parameters quoted by Gogia and Burton, and obtain one of similar dimensions

Gogia, G. and Burton, J. (2017). Emergent Bistability and Switching in a Nonequilibrium Crystal. *Physical Review Letters*, 119(17).

Choice of System Parameters



- We simulate a crystal using parameters quoted by Gogia and Burton, and obtain one of similar dimensions
- We simulate the distribution of mass and charge that they claim leads to self-organizational behavior

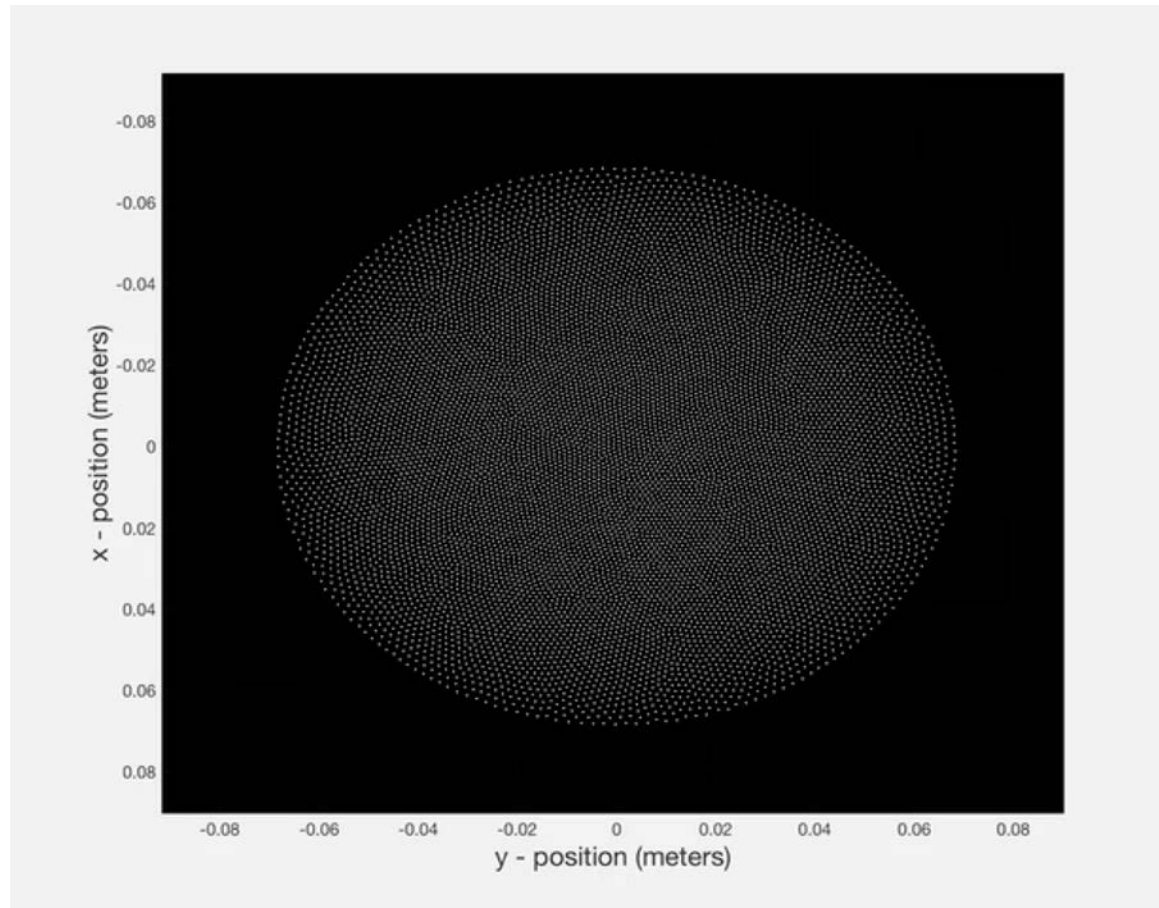
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Choice of System Parameters



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- We simulate the distribution of mass and charge that they claim leads to self-organizational behavior
- And...

Simulation



Simulation Results



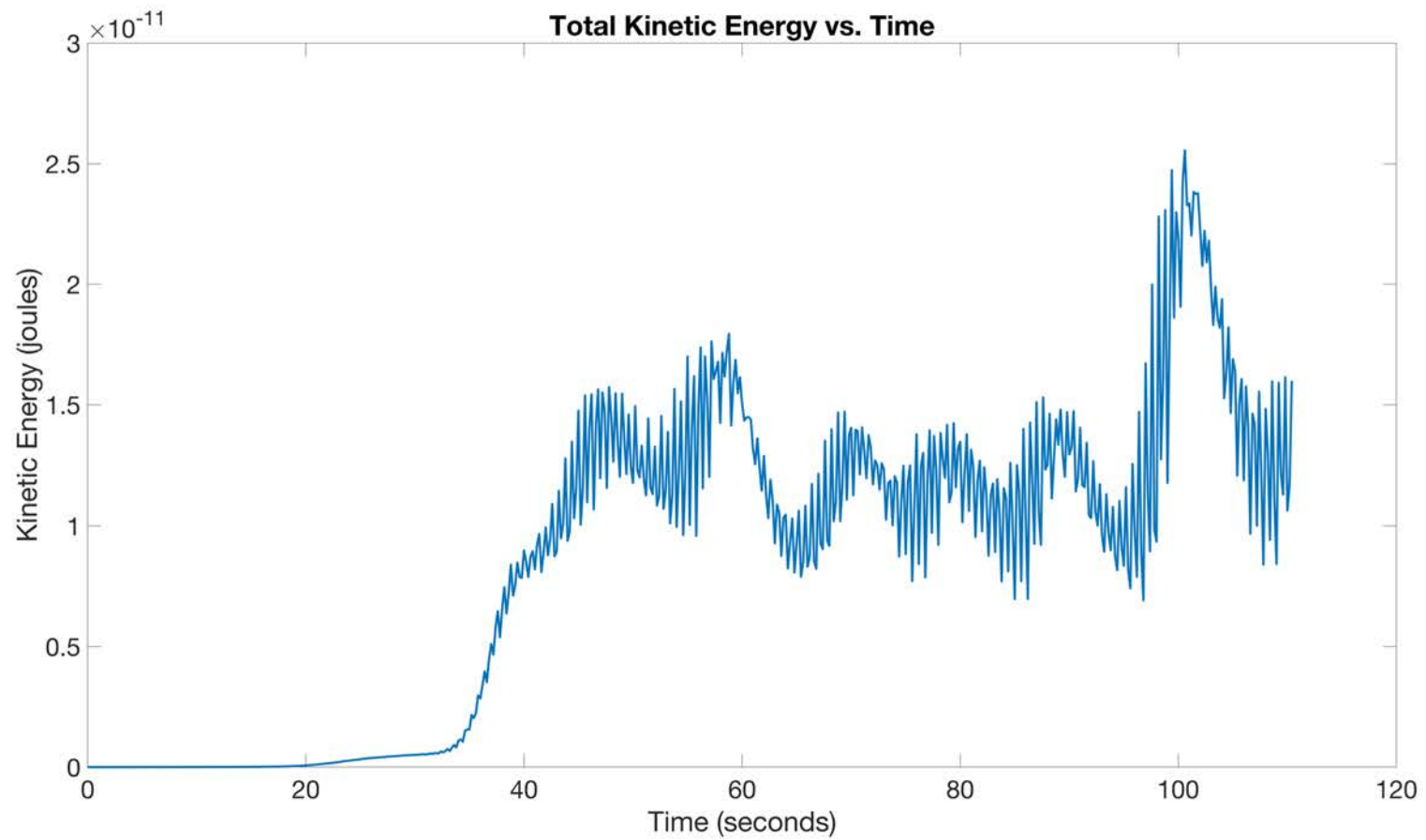
- We simulate a crystal using parameters quoted by Gogia and Burton, and obtain one of similar dimensions
- We simulate the distribution of mass and charge that they claim leads to self-organizational behavior
- And...we never seem to re-organize

Simulation Results



- This different dynamical behavior is likely due to a different confinement in the z-direction

Simulation Results



Future Work

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- Diffusive behavior is predicted for certain ranges of the coupling parameter
- Therefore, it's crucial to be able to simulate reliably at constant temperatures

Future Work



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- Simulate conditions leading to subdiffusion and superdiffusion
 - Implement Lévy-stable distributions in `box_tree` to determine which lead to subdiffusion and superdiffusion
- Adjust simulation parameters to observe self-organizational phenomena

Thank you for your attention!

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